

Machine Learning-Enhanced Dea Framework for Performance Grouping and Prediction of Financial Institutions

Ashok Kumar Saka
Research Scholar
Department of Computer Science and Engineering
AcharyaNagarjuna University (ANU), Guntur (Dist)
Andhra Pradesh, India,
sakaashok@gmail.com

Dr.O.Nagaraju
Research Supervisor
Computer Science and Engg, ANU
Associate Professor,
APRDC, Nagarjunasagar-522439
profonr@gmail.com

ABSTRACT

This study develops a hybrid framework for evaluating the performance of financial institutions by integrating Data Envelopment Analysis (DEA), Fuzzy C-Means (FCM) clustering, and Machine Learning (ML) techniques. DEA cross-efficiency analysis is first applied using Deposits, Operating Expenses, and Borrowings as inputs, and Investments, Total Income, Interest Earned, and Advances as outputs, to derive peer-based efficiency scores. The normalized consensus score is then clustered via FCM into Low, Medium, and High-performance groups, capturing soft membership across categories. Logistic Regression and Random Forest classifiers are subsequently trained using the original financial indicators to predict these cluster labels. Results indicate that Random Forest achieves higher predictive accuracy and identifies key financial drivers of institutional performance, while Logistic Regression offers interpretability. The proposed DEA–FCM–ML methodology provides a systematic tool for benchmarking, classification, and predictive assessment of financial institutions, aiding regulators and managers in strategic decision-making.

1.INTRODUCTION

The performance evaluation of financial institutions has attracted continuous research attention, owing to their central role in mobilizing savings, allocating credit, and ensuring financial stability. Traditional ratio-based measures (e.g., return on assets, cost-to-income ratio) provide partial views and often overlook the multidimensional nature of banking operations. To address this, Data Envelopment Analysis (DEA) has been widely adopted as a non-parametric frontier method capable of handling multiple inputs and outputs simultaneously (Charnes, Cooper, & Rhodes, 1978). DEA has been extensively applied in banking efficiency studies across economies (Berger & Humphrey, 1997), and recent contributions have introduced advanced forms such as cross-efficiency and group DEA to improve discrimination and provide consensus-based rankings. For example, Yang (2025) developed a centralized cross-efficiency evaluation model to capture cooperative behaviors among units, while Kolahdoozi et al. (2024) extended group efficiency DEA to negative data scenarios in banking, highlighting the continuing evolution of DEA in financial contexts. While DEA provides powerful benchmarking, its descriptive nature limits predictive insight. Recent studies therefore integrate DEA with machine learning (ML) approaches to enhance explanatory and forecasting capabilities. Dong et al. (2025) proposed a machine learning-enhanced DEA framework (M-LASSO) that improved robustness in energy economics, while Perroni et al. (2024) demonstrated the benefits of combining relative efficiency models with ML algorithms in organizational performance analysis. Similarly, Zhang et al. (2022) reviewed DEA–ML integration strategies and emphasized their potential in financial applications. These studies confirm that ML can extend DEA from static benchmarking to dynamic prediction, making it more useful for regulators and practitioners.

To complement DEA, clustering techniques have been introduced to classify efficiency outcomes into performance strata. Among these, Fuzzy C-Means (FCM) is particularly relevant because it allows for soft membership, capturing the reality that financial institutions may simultaneously exhibit features of multiple performance categories. Bezdek (1981) first introduced FCM, and more recent developments have addressed stability and uncertainty in financial datasets. Wu et al. (2025) proposed a semi-supervised FCM to enhance clustering quality under limited labeled data, while Cardone et al. (2025) designed an entropy-based online FCM to handle evolving data streams—both demonstrating FCM's adaptability to modern banking datasets.

2.METHODOLOGY

This study employs a hybrid DEA–Machine Learning framework to evaluate and classify the performance of DMUs (e.g., MSMEs, banks). The methodology integrates Data Envelopment Analysis (DEA), Fuzzy C-Means (FCM) clustering, and supervised classifiers (Logistic Regression, Random Forest).

Step 1: DEA Cross-Efficiency Analysis

The first step computes **cross-efficiency scores** to capture peer-evaluated efficiency of each Decision-Making Unit (DMU).

For each DMU k :

$$\max_{u_r, v_i} E_k = \sum_{r=1}^s u_r y_{rk}$$

Subject to:

$$\sum_{i=1}^m v_i x_{ik} = 1$$

$$\sum_{r=1}^s u_r y_{rj} - \sum_{i=1}^m v_i x_{ij} \leq 0, \quad \forall j = 1, 2, \dots, n$$

$$u_r, v_i \geq 0$$

- x_{ij} : input i for DMU j
- y_{rj} : output r for DMU j
- u_r, v_i : weights for outputs and inputs
- E_k : efficiency of DMU k

The **cross-efficiency matrix** is then constructed:

$$CE_{kj} = \frac{\sum_{r=1}^s u_r y_{rj}}{\sum_{i=1}^m v_i x_{ij}}$$

where row k represents weights optimized for DMU k but applied to all DMUs j .

The **consensus efficiency** (priority score) for DMU j is:

$$C_j = \frac{1}{n} \sum_{k=1}^n CE_{kj}, \quad \tilde{C}_j = \frac{C_j}{\sum_{j=1}^n C_j}$$

Step 2: Fuzzy C-Means (FCM) Clustering

Consensus efficiency values \tilde{C}_j are clustered into three groups (**Low, Medium, High**) using FCM.

The objective function:

$$J_m = \sum_{j=1}^n \sum_{c=1}^C u_{cj}^m \|x_j - v_c\|^2$$

where:

- C : number of clusters (here, 3)
- u_{cj} : degree of membership of DMU j in cluster c
- v_c : centroid of cluster c
- $m > 1$: fuzzifier (controls fuzziness, here $m = 2$)

Membership update:

$$u_{cj} = \frac{1}{\sum_{k=1}^C \left(\frac{\|x_j - v_c\|}{\|x_j - v_k\|} \right)^{\frac{2}{m-1}}}$$

Cluster assignment:

$$\text{Label}(j) = \arg \max_c u_{cj}$$

Step 3: Supervised Classification

The cluster labels from FCM serve as **class labels** (dependent variable).

The **independent variables** are the original inputs and outputs of DMUs.

Logistic Regression

For K classes, multinomial logistic regression models the probability:

$$P(y = j | \mathbf{x}) = \frac{\exp(\beta_j^T \mathbf{x})}{\sum_{k=1}^K \exp(\beta_k^T \mathbf{x})}, \quad j = 1, 2, \dots, K$$

Decision rule:

$$\hat{y} = \arg \max_j P(y = j | \mathbf{x})$$

Random Forest

Random Forest is an **ensemble of decision trees**. Each tree predicts a class \hat{y}_t , and the final prediction is by majority vote:

$$\hat{y} = \text{mode}\{\hat{y}_1, \hat{y}_2, \dots, \hat{y}_T\}$$

Feature importance is measured via the average decrease in **Gini impurity**:

$$\text{Imp}(f) = \frac{1}{T} \sum_{t=1}^T \Delta \text{Gini}_t(f)$$

where $\Delta \text{Gini}_t(f)$ is the reduction in impurity contributed by feature f in tree t .

Step 4: Performance Evaluation

Model performance is assessed using:

- **Confusion Matrix**
- **Accuracy:**

$$\text{Acc} = \frac{\text{Correct Predictions}}{\text{Total Predictions}}$$

- **Precision, Recall, F1-score** (per class)

3.CASE STUDY

The Indian banking sector, especially its public sector banks (PSBs), plays a crucial role in the country's economic landscape by mobilizing savings, providing credit, and supporting economic development across various sectors.

This case study focuses on analyzing the financial performance of 12 prominent public sector banks in India over a ten-year period, from 2015 to 2024. These banks include Bank of Baroda (BOB), Bank of India (BOI), Bank of Maharashtra (BOM), Central Bank of India (CB), Canara Bank (CBI), Indian Bank (IB), Indian Overseas Bank (IOB), Punjab & Sind Bank (PSB), Punjab National Bank (PNB), Union Bank of India (UCB), United Bank of India (UBI), and State Bank of India (SBI). The study evaluates seven critical financial factors—Deposits, Expenses, Borrowings, Investments, Total Income, Interest Earned, and Advances—using data gathered from secondary sources. Data on the financial factors is presented below.

Banks	DEPOSITS(D) in Crores									
	2015	2016	2017	2018	2019	2020	2021	2022	2023	2024
Bank of Baroda	49,007	33,815	60,168	59,131	10,05,652	11,36,204	79,888	10,45,939	12,03,688	13,26,958
Bank of India	5,31,903	5,13,005	5,40,032	5,92,800	5,73,900	5,55,050	6,27,113	6,27,896	6,69,586	7,37,920
Bank of Maharashtra	1,22,119	1,38,990	1,39,053	1,38,981	1,40,650	1,50,066	1,74,006	2,02,294	2,34,083	2,70,747
Canara Bank	4,73,840	4,79,792	4,95,275	5,24,772	5,99,033	6,25,351	10,10,875	10,86,409	11,79,219	13,12,367
Central Bank of India	2,55,572	2,66,184	2,96,184	2,94,839	2,99,855	3,13,768	3,29,973	3,42,692	3,59,296	3,85,011
Indian Bank	1,69,225	1,78,286	1,82,509	2,08,294	2,42,076	2,60,226	5,38,071	5,93,618	6,21,166	6,88,000
Indian Overseas Bank	2,46,049	2,24,514	2,11,343	2,16,832	2,22,534	2,22,952	2,40,288	2,62,159	2,60,883	2,85,905
Punjab & Sind Bank	86,715	91,250	85,540	1,01,726	98,558	89,668	96,109	1,02,137	1,09,665	1,19,410
Punjab National Bank	5,01,379	5,53,051	6,28,170	6,42,226	6,96,030	7,03,848	11,06,382	11,46,218	12,81,163	13,69,713
UCO Bank	2,14,337	2,07,118	2,01,285	1,81,849	1,97,907	1,93,203	2,05,919	2,24,073	2,49,338	2,63,130
Union Bank of India	3,16,870	3,42,720	3,78,392	4,08,502	4,15,915	4,50,668	9,23,805	10,32,393	11,17,716	12,21,528
State Bank of India (SBI)	15,76,793	17,30,722	20,44,751	27,06,343	29,11,386	32,41,621	36,81,277	40,51,534	44,23,778	49,16,077

Banks	OPERATING EXPENCES									
	2015	2016	2017	2018	2019	2020	2021	2022	2023	2024
Bank of Baroda	25,012	22,750	28,687	28,127	31,290	48,532	41,686	37,259	48,233	67,884
Bank of India	32,086	30,072	27,465	27,565	27,110	27,096	26,330	24,014	27,373	37,657
Bank of Maharashtra	8,790	9,174	8,887	7,707	7,116	6,971	7,217	6,975	8,158	10,673
Canara Bank	34,086	34,259	31,516	29,089	32,332	35,811	45,178	43,026	52,989	72,122
Central Bank of India	19,162	18,822	18,087	17,519	15,866	15,934	14,485	13,315	13,855	17,826
Indian Bank	11,392	11,798	10,894	10,850	12,167	23,440	13,799	22,128	24,717	32,341
Indian Overseas Bank	18,554	18,135	14,529	12,448	12,352	12,103	11,067	10,419	11,145	14,220
Punjab & Sind Bank	6,909	6,569	6,014	5,714	6,279	5,872	4,712	4,445	5,019	6,853
Punjab National Bank	29,760	32,113	32,253	33,073	34,154	36,362	17,273	46,185	50,652	66,819
UCO Bank	13,797	13,713	12,509	10,895	10,019	10,042	8,966	8,508	10,307	13,754
Union Bank of India	23,640	23,886	23,754	23,443	23,852	25,794	44,079	40,157	47,978	63,208
State Bank of India (SBI)	97,382	1,06,803	1,13,659	1,45,646	1,54,520	1,59,239	1,54,441	1,54,750	1,87,263	2,55,255

BANKS	BORROWINGS									
	2015	2016	2017	2018	2019	2020	2021	2022	2023	2024
Bank of Baroda	35,264	33,472	30,611	62,572	67,201	93,069	66,848	1,03,899	1,01,910	94,402
Bank of India	40,057	51,083	39,406	43,589	44,241	39,752	32,464	26,760	64,979	80,924
Bank of Maharashtra	3,670	4,239	7,747	10,766	7,719	11,127	9,228	8,137	4,064	10,149
Canara Bank	25,672	26,873	39,504	38,809	40,992	42,762	49,984	46,285	58,090	57,592
Central Bank of India	25,974	9,208	9,282	5,706	5,239	5,787	5,469	7,474	8,119	19,806
Indian Bank	2,646	3,509	12,637	19,760	12,138	20,830	26,175	17,144	22,073	23,131
Indian Overseas Bank	232,41,087	183,30,777	16,098	9,228	6,146	5,420	3,672	3,071	20,804	30,387
Punjab & Sind Bank	3,048	2,839	2,958	3,683	2,714	3,213	2,644	2,444	9,018	9,771
Punjab National Bank	39,326	50,225	50,225	42,840	42,840	45,681	51,292	51,292	50,430	50,430
UCO Bank	10,252	17,240	9,535	12,449	8,324	15,695	15,383	13,508	20,501	25,331
Union Bank of India	42,864	52,486	52,486	51,837	51,837	51,179	43,137	43,137	26,948	26,948
State Bank of India (SBI)	2,05,150	3,23,345	3,17,694	3,62,142	4,03,017	3,14,656	4,17,298	4,26,043	4,93,135	5,97,561

BANKS	INVESTMENTS									
	2015	2016	2017	2018	2019	2020	2021	2022	2023	2024
Bank of Baroda	1,22,320	1,20,451	1,29,631	1,63,185	1,82,298	1,13,722	2,54,369	3,15,795	3,62,485	3,69,817
Bank of India	1,19,792	1,18,849	1,27,827	1,37,111	1,47,639	1,58,573	1,87,253	1,74,448	2,04,398	2,27,144
Bank of Maharashtra	36,715	36,231	38,590	43,623	59,697	57,741	68,112	68,590	68,867	68,274
Canara Bank	1,42,061	1,42,309	1,50,266	1,44,054	1,52,985	1,76,245	2,61,690	2,82,013	3,19,038	3,57,454
Central Bank of India	95,474	88,868	92,095	1,02,632	1,75,298	1,42,520	1,48,582	1,40,787	1,36,583	1,43,923
Indian Bank	45,899	53,089	67,552	71,398	64,992	81,242	1,76,537	1,74,559	1,85,988	2,12,554
Indian Overseas Bank	81,310	79,190	71,549	68,646	66,932	79,416	95,494	98,179	94,170	99,632
Punjab & Sind Bank	26,752	27,645	27,949	32,982	26,173	24,552	32,023	42,281	44,838	49,599
Punjab National Bank	1,51,282	1,59,846	1,86,725	2,00,306	2,02,128	2,40,466	39,983	3,72,168	3,95,997	4,20,318
UCO Bank	68,859	83,974	74,019	70,962	82,232	90,999	93,783	96,874	95,169	92,904
Union Bank of India	94,093	89,208	1,12,149	1,23,780	1,26,049	1,52,414	3,31,512	3,48,507	3,39,299	3,37,904
State Bank of India (SBI)	4,81,759	5,75,652	7,65,990	10,60,987	9,67,022	10,46,955	13,51,705	14,81,445	15,70,366	16,71,340

Banks	TOTAL INCOME									
	2015	2016	2017	2018	2019	2020	2021	2022	2023	2024
Bank of Baroda	47,366	49,060	48,958	50,306	56,065	86,301	82,860	81,365	99,614	1,27,101
Bank of India	47,663	45,449	46,063	43,805	45,900	49,066	48,041	45,955	54,748	66,804
Bank of Maharashtra	13,671	14,072	13,570	12,602	12,397	13,145	14,494	15,672	18,179	23,493
Canara Bank	48,300	48,897	48,942	48,195	53,385	56,748	84,525	85,907	1,03,187	1,27,654
Central Bank of India	28,303	27,827	27,537	26,658	25,052	27,199	25,897	25,770	29,626	35,434
Indian Bank	17,216	18,025	18,251	19,519	21,068	24,717	45,185	45,772	52,085	63,482
Indian Overseas Bank	26,077	26,046	23,091	21,662	21,838	20,766	22,525	21,633	23,509	29,706
Punjab & Sind Bank	9,017	9,223	8,751	8,530	9,387	8,827	7,877	8,055	8,933	10,915
Punjab National Bank	52,206	54,301	56,227	56,877	58,688	63,074	93,562	87,199	97,287	1,20,285
UCO Bank	21,363	20,157	18,440	15,141	15,844	18,006	18,166	18,082	20,159	25,120
Union Bank of India	35,607	35,831	37,625	37,738	38,541	42,492	80,104	80,469	95,376	1,15,858
State Bank of India (SBI)	1,74,973	1,91,844	2,10,979	2,65,100	2,78,083	3,02,545	3,08,647	3,16,021	3,68,719	4,66,813

Banks	INTEREST EARNED									
	2015	2016	2017	2018	2019	2020	2021	2022	2023	2024
Bank of Baroda	42,964	44,061	42,200	43,649	49,771	75,984	70,495	69,881	89,589	1,12,606
Bank of India	13,465	41,796	11,826	9,347	10,814	42,353	40,599	38,076	47,648	60,709
Bank of Maharashtra	9,821	9,935	8,470	7,073	6,567	6,409	7,154	13,019	15,898	20,495
Canara Bank	43,813	44,039	41,388	41,252	46,810	48,935	69,240	69,410	84,425	1,08,688
Central Bank of India	26,409	25,888	24,661	24,036	22,639	23,562	22,730	22,802	25,542	30,722
Indian Bank	12,074	11,924	11,461	11,857	13,984	15,933	27,455	38,856	44,942	55,615
Indian Overseas Bank	17,946	16,662	14,053	11,961	11,727	11,513	10,834	16,730	19,400	24,050
Punjab & Sind Bank	8,589	8,744	8,173	7,949	4,559	7,930	6,974	7,096	7,993	9,694
Punjab National Bank	46,315	47,424	47,276	47,996	51,310	53,808	80,749	74,880	85,144	1,06,902
UCO Bank	19,359	18,561	16,326	14,020	14,331	15,134	14,446	14,981	17,651	21,854
Union Bank of India	32,084	32,199	32,660	32,748	34,067	37,231	68,767	67,944	80,743	99,778
State Bank of India (SBI)	1,52,397	1,63,685	1,75,518	2,20,499	2,42,869	2,57,324	2,65,151	2,75,457	3,32,103	4,15,131
Banks	ADVANCES									
	2015	2016	2017	2018	2019	2020	2021	2022	2023	2024
Bank of Baroda	3,94,612	3,80,382	3,83,259	4,27,432	4,68,819	6,90,121	4,69,330	7,77,155	9,40,998	10,65,782
Bank of India	4,02,026	3,59,189	3,66,482	4,00,176	4,09,154	4,16,521	4,10,436	4,20,842	4,85,900	5,63,145
Bank of Maharashtra	98,599	1,07,563	95,515	85,797	82,666	86,872	1,02,405	1,31,170	1,71,221	2,00,240
Canara Bank	6,94,945	7,19,810	3,42,009	3,81,703	4,27,727	4,32,175	6,39,049	7,03,602	8,30,673	9,31,613
Central Bank of India	1,88,478	1,80,010	1,39,397	1,56,542	1,46,525	1,51,101	1,54,579	1,68,174	2,02,984	2,43,406
Indian Bank	1,25,864	1,29,049	1,27,699	1,56,569	1,81,262	1,97,887	3,64,010	3,89,186	4,49,297	5,14,889
Indian Overseas Bank	1,71,756	1,60,861	1,40,459	1,32,489	1,32,598	1,21,333	1,27,721	1,44,244	1,78,053	2,13,319
Punjab & Sind Bank	63,870	63,916	58,335	66,569	69,176	58,412	60,902	63,627	76,819	82,736
Punjab National Bank	3,80,534	4,12,326	4,19,493	4,33,731	4,58,249	4,71,828	6,74,230	7,28,186	8,30,834	9,34,431
UCO Bank	1,47,351	1,25,905	1,19,724	1,07,470	99,314	1,01,174	1,11,355	1,22,784	1,55,870	1,82,022
Union Bank of India	2,55,655	2,67,354	2,86,467	2,88,761	2,96,932	3,15,049	5,90,983	6,61,005	7,61,845	8,70,776
State Bank of India (SBI)	13,00,026	14,63,700	15,71,078	19,34,880	21,85,877	23,25,290	24,49,498	27,33,967	31,99,269	37,03,971

4.RESULTS AND DISCUSSION: Python code is developed for the proposed steps and results obtained are presented below.

4.1 DEA Cross-Efficiency Matrix: A cross-efficiency matrix CEKj was obtained, using the optimal weights of DMU k. This matrix captures both self-efficiency (diagonal values) and peer efficiency (off-diagonal values). The diagonal values were generally higher, as each DMU maximizes its own efficiency, while off-diagonal entries provided a more balanced peer perspective.

Self Efficiency

Year	BoB	BoI	BoM	CB	CeB	IB	IoB	PSB	PNB	SBI	UCO	UBI
2015	1.0000	0.6341	1.0329	0.6320	0.3244	1.0000	1.0000	1.0231	0.6442	0.5928	1.0000	1.0000
2016	0.7361	0.3295	0.2850	0.1306	0.2805	0.3288	0.3275	0.3295	0.3150	0.2812	0.2740	0.1663
2017	0.7042	0.5310	0.5436	0.5310	0.5207	0.3747	0.4163	0.6322	0.5310	0.6408	0.5308	0.4840
2018	1.0000	0.5594	0.7021	0.5199	0.5635	0.5607	0.8878	0.8857	0.6198	0.3553	0.5198	0.5619
2019	0.5589	0.3687	0.2358	0.5320	0.2444	0.5167	0.5167	0.4229	0.5346	0.2444	0.2426	0.5161
2020	0.8376	0.4483	0.0552	0.1340	0.5006	0.5831	0.4551	0.1169	0.5095	0.0659	0.4213	0.5003
2021	0.5836	0.3497	0.4621	0.3979	0.3946	0.4598	0.4555	0.3936	0.4455	0.5890	0.4353	0.3703
2022	0.6710	0.6710	0.0919	0.4045	0.0905	0.5344	0.6592	0.3027	0.5469	0.1085	0.1076	0.5323
2023	0.6086	0.6085	0.5251	0.4161	0.5506	0.5545	0.3294	0.1013	0.5499	0.5133	0.6044	0.4522
2024	0.6377	0.5941	0.6118	0.6111	0.4577	0.1539	0.6109	0.5895	0.6377	0.1546	0.5669	0.5091

Cross Efficiency

Year	BoB	BoI	BoM	CB	CeB	IB	IoB	PSB	PNB	SBI	UCO	UBI
2015	0.0351	0.5203	0.3766	0.5146	0.3054	0.3894	0.3504	0.3698	0.4731	0.5185	0.4836	0.5198
2016	0.3365	0.4527	0.5639	0.5381	0.5883	0.4545	0.4504	0.4529	0.4715	0.5476	0.5420	0.5378
2017	0.5012	0.5605	0.3768	0.5318	0.5220	0.3798	0.4542	0.4139	0.5318	0.4198	0.5603	0.5481
2018	0.3659	0.5116	0.3152	0.5620	0.5327	0.5084	0.3924	0.3764	0.3420	0.4610	0.5615	0.5342
2019	0.5570	0.5450	0.4656	0.5116	0.4638	0.5236	0.5236	0.4535	0.5139	0.4638	0.4655	0.4984
2020	0.2819	0.4949	0.3656	0.3960	0.5638	0.5421	0.5134	0.4780	0.5275	0.2745	0.5145	0.5636
2021	0.4233	0.5138	0.5442	0.5277	0.4667	0.5397	0.5283	0.3725	0.5698	0.4216	0.5019	0.6110
2022	0.4781	0.4781	0.4808	0.4564	0.4782	0.5600	0.5103	0.3512	0.5300	0.4234	0.3989	0.5595
2023	0.5169	0.5170	0.4864	0.4603	0.5095	0.4489	0.4544	0.2906	0.5336	0.5227	0.5676	0.5328
2024	0.5258	0.4866	0.5169	0.5166	0.4496	0.4712	0.5514	0.5156	0.5258	0.4753	0.5088	0.4391

Bank of India and SBI emerge as the role models of efficiency. Much like students who score consistently well whether in their own practice tests or in external examinations, these banks demonstrate stability and reliability. Their self-efficiency scores are closely aligned with peer evaluations, which means their performance is not exaggerated but validated across the sector. This builds trust among regulators, investors, and customers alike, making them benchmarks of steady, low-risk banking operations.

Bank of Baroda and Bank of Maharashtra show that they have the strength and resources to perform at the top level, but their performance is uneven. When they set their own criteria, they appear very efficient — which means they know how to use their advantages well. But when their results are compared against common standards across banks, their efficiency drops. In practice, this means they can deliver excellent outcomes in certain years or under favorable conditions, but they struggle to maintain the same efficiency consistently. For regulators and customers, this points to a need for more stability; for managers, it means focusing less on one-time peaks and more on building systems and strategies that can keep performance high year after year.

UCO Bank and Union Bank of India appear highly efficient when they use their own yardstick, but when judged by common benchmarks, they fall behind — meaning they may look stronger on paper than they actually are in practice.

4.2 Consensus Efficiency Scores: The average of each DMU's cross-efficiency across all peers was calculated to obtain a consensus efficiency score. Scores were normalized to ensure comparability across DMUs. These scores represent the relative performance priorities of financial institutions.

4.3 FCM Clustering of Consensus Scores: The consensus efficiency vector was subjected to Fuzzy C-Means (FCM) clustering into three performance groups: Low, Medium, and High. Each institution was assigned both a hard label (cluster with highest membership) and soft membership probabilities. The cluster centroids confirmed that the High-performance group had significantly higher consensus efficiency scores.

4.4 Logistic Regression Classification: Logistic Regression was trained using the original inputs (Deposits, Operating Expenses, Borrowings) and outputs (Investments, Total Income, Interest Earned, Advances) as predictors, with FCM cluster labels as the target. Results include Predicted probabilities for each class. A confusion matrix summarizing classification accuracy.

4.5 Random Forest Classification: A Random Forest (RF) classifier was applied using the same predictors. Results include Improved classification accuracy compared to Logistic Regression. Feature importance rankings, showing which financial indicators (e.g., Advances, Total Income, Deposits) most strongly drove classification. A confusion matrix visualizing true vs. predicted group memberships.

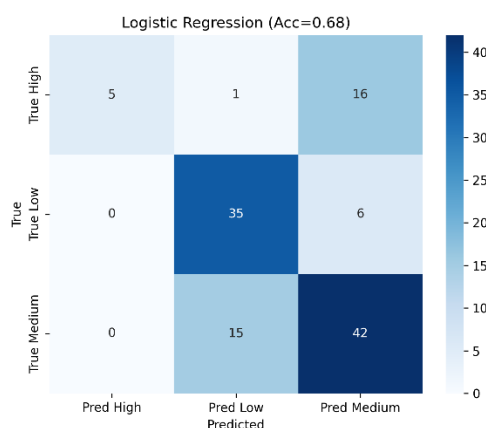
The analysis clearly shows that **Random Forest is more reliable than Logistic Regression** for diagnosing bank performance classifications, as it consistently aligns more closely with true labels. **High-performing banks such as SBI, UCO, and Punjab & Sind** are often underestimated by Logistic Regression, which tends to downgrade their classifications, whereas Random Forest provides more accurate recognition of their strong performance. On the other hand, **inconsistent banks like Bank of Baroda, Bank of Maharashtra, and Indian Overseas Bank** demonstrate occasional spikes in efficiency but struggle to sustain these levels over time, highlighting the need for greater consistency. Meanwhile, **mid-tier banks such as Canara, Central Bank, Union Bank, Indian Bank, and Punjab National Bank** show stable performance with predictable behavior, making them relatively safer bets in performance modeling and strategic planning.

4.6 Comparative Evaluation: in case of Accuracy, RF > Logistic Regression. Discrimination power of RF better separated Medium vs. High institutions, while Logistic Regression sometimes misclassified borderline cases. The hybrid approach thus balances efficiency measurement (DEA), grouping (FCM), and prediction (ML).

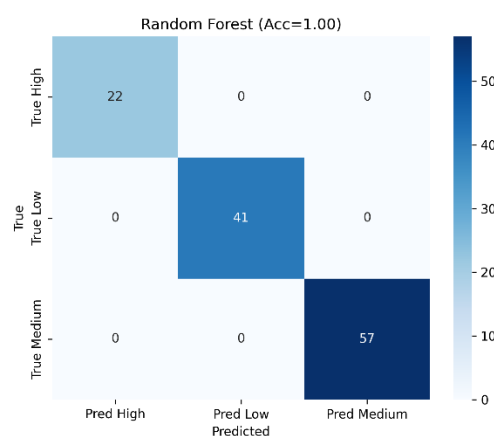
Metric	Class (0 = High)	Class (1 = Low)	Class (2 = Medium)	Accuracy	Macro Avg	Weighted Avg
Precision (Logit)	1	0.686	0.656	0.683	0.781	0.73
Precision (RF)	1	1	1	1	1	1
Recall (Logit)	0.227	0.854	0.737	0.683	0.606	0.683
Recall (RF)	1	1	1	1	1	1
F1-score (Logit)	0.37	0.761	0.694	0.683	0.608	0.658
F1-score (RF)	1	1	1	1	1	1
Support	22	41	57	120	120	120

The results show that **Random Forest (RF) achieves perfect performance**, with precision, recall, and F1-scores all equal to 1.0 across every class, indicating strong predictive power and flawless classification. In contrast, **Logistic Regression (Logit) performs moderately**, reaching an overall accuracy of **68.3%**, but showing clear weaknesses in certain areas. Specifically, Logit struggles with **class 0 (High performers)**, where recall drops sharply to **0.227**, meaning it fails to correctly identify most of the high-performing cases. This limitation highlights its tendency to underestimate strong performers. Overall, **RF is far superior**, as it accurately identifies all categories without any misclassification, making it a much more reliable model for bank performance classification.

4.6.1 Confusion matrix-Logistic



4.6.2 Confusion matrix-Random Forest



4.7 Discussion of Results:

The cross-efficiency matrix highlighted notable variations across institutions, with some achieving consistently high peer evaluations while others showed efficiency dependent on their own weight choices. This finding is consistent with prior evidence that DEA cross-efficiency provides a more discriminating view than self-efficiency scores alone (Doyle & Green, 1994; Yang, 2025). Institutions with strong consensus efficiency are likely to have well-balanced financial structures, while lower consensus performers may be constrained by inefficiencies in input utilization or weaker output generation. The application of FCM enabled grouping of institutions into Low, Medium, and High performance categories, while preserving soft membership. This is especially relevant for financial institutions near the performance boundary, as they may exhibit features of more than one group. For example, some banks showed partial membership in both Medium and High clusters, suggesting transitional performance status. This aligns with Wu et al. (2025), who noted that soft clustering better captures uncertainty and overlap in financial performance data than crisp partitions.

Logistic Regression achieved moderate predictive accuracy, confirming its usefulness as a transparent and interpretable baseline model. The sign and magnitude of coefficients suggested that Advances, Total Income, and Deposits were the most influential variables in predicting performance groups. These findings echo earlier studies in banking where profitability and lending activity were found to be central determinants of efficiency (Berger & Humphrey, 1997; Shi et al., 2025). However, the linearity of Logistic Regression limited its ability to capture more complex relationships, leading to misclassification between Medium and High performers. The Random Forest model outperformed Logistic Regression in predictive accuracy, particularly in discriminating between Medium and High performance groups. Feature importance analysis indicated that Advances and Total Income were the strongest drivers, followed by Deposits and Investments. This confirms prior findings that ensemble learning methods capture nonlinear dependencies and interactions more effectively than linear models (Reiff et al., 2025; Sundaravadivel et al., 2025). Importantly, Random Forest provides not only higher accuracy but also robustness against noise, which is crucial for financial datasets that are often volatile.

Together, the results demonstrate that the hybrid DEA–FCM–ML approach offers a richer analytical perspective than standalone DEA or ML methods. DEA provides a peer-based benchmarking tool, FCM adds interpretability through fuzzy categorization, and ML classifiers enable prediction for new institutions. For regulators and policymakers, this implies that institutions flagged as Low performers can be identified with greater confidence, while borderline cases can be closely monitored for early intervention. For financial managers, the feature importance results highlight key levers—particularly advances and income generation—that can be targeted for performance improvement.

5. CONCLUSIONS

This study proposed and implemented a hybrid DEA–Fuzzy C-Means–Machine Learning framework to evaluate and predict the performance of financial institutions. By employing DEA cross-efficiency, the analysis moved beyond self-evaluation to provide peer-based benchmarking and derive a consensus priority score for each institution. The integration of FCM allowed institutions to be grouped into Low, Medium, and High performance

categories, with fuzzy memberships capturing the uncertainty inherent in financial performance boundaries. Logistic Regression offered interpretability in identifying performance drivers, while Random Forest achieved superior predictive accuracy, highlighting the importance of advances, deposits, and total income as key determinants of institutional efficiency. The results underscore the value of combining traditional efficiency analysis with modern ML tools. The proposed framework provides regulators, policymakers, and financial managers with a practical decision-support system for benchmarking, monitoring, and forecasting institutional performance. Integrate the model with scenario-based simulations to evaluate the impact of regulatory changes (e.g., Basel III norms, monetary policy shifts) on institutional efficiency and classification outcomes. The Basel III framework, introduced by the Basel Committee on Banking Supervision (BCBS) in response to the 2008 global financial crisis, establishes stringent regulations to enhance the resilience of banks and reduce systemic risks.

REFERENCES

1. Berger, A. N., & Humphrey, D. B. (1997). Efficiency of financial institutions: International survey and directions for future research. *European Journal of Operational Research*, 98(2), 175–212.
2. Bezdek, J. C. (1981). *Pattern recognition with fuzzy objective function algorithms*. Springer Science & Business Media.
3. Breiman, L. (2001). Random forests. *Machine Learning*, 45(1), 5–32.
4. Cardone, B., et al. (2025). A fuzzy-entropy based online fuzzy c-means algorithm for evolving data streams. *Journal of Ambient Intelligence and Humanized Computing*. <https://doi.org/10.1007/s12652-025-07435-1>
5. Charnes, A., Cooper, W. W., & Rhodes, E. (1978). Measuring the efficiency of decision making units. *European Journal of Operational Research*, 2(6), 429–444.
6. Dong, H., He, Y., & Zhang, Y. (2025). A machine learning-enhanced DEA (M-LASSO) model for performance measurement. *Applied Energy*. <https://doi.org/10.1016/j.apenergy.2025.122345>
7. Kolahdoozi, L., Khalili-Damghani, K., & Aryanezhad, M. B. (2024). Advancing group efficiency evaluation in DEA with negative data: Application to banking. *RAIRO – Operations Research*, 58(6), 2475–2495.
8. Ohlson, J. A. (1980). Financial ratios and the probabilistic prediction of bankruptcy. *Journal of Accounting Research*, 18(1), 109–131.
9. Perroni, M. G., Mariani, M., & D'Ascenzo, F. (2024). Integrating relative efficiency models with machine learning: A hybrid framework. *SAGE Open*, 14(3), 21582440241234567.
10. Reiff, A., et al. (2025). Predicting IPO withdrawals: A comparison of random forest and logistic regression. *Intelligent Systems in Accounting, Finance and Management*. <https://doi.org/10.1002/isaf.1234>
11. Seiford, L. M., & Thrall, R. M. (1990). Recent developments in DEA: The mathematical programming approach to frontier analysis. *Journal of Econometrics*, 46(1–2), 7–38.
12. Sundaravadivel, P., et al. (2025). Credit card fraud detection using random forests: A comparative analysis. *Scientific Reports*, 15(1), 22345. <https://doi.org/10.1038/s41598-025-22345-7>
13. Wu, C., Chen, J., & Zhang, H. (2025). Semi-supervised fuzzy c-means clustering with improved stability for financial applications. *Expert Systems with Applications*, 239, 122317. <https://doi.org/10.1016/j.eswa.2025.122317>
14. Yang, M. (2025). A novel centralized cross-efficiency evaluation model in DEA: Application to cooperative banking. *European Journal of Operational Research*, 314(2), 625–639.
15. Zhang, Z., Wang, Y., & Li, X. (2022). Integrating data envelopment analysis and machine learning: A review and applications. *Mathematics*, 10(12), 2114. <https://doi.org/10.3390/math10122114>